

8)

$$I = \frac{P}{4\pi r^2}$$

a) $L = L_0 \log \frac{I}{I_0}$ where $L_0 = 10 \text{ dB}$

$$L = L_0 \log \left[\frac{\frac{P}{4\pi r^2}}{I_0} \right]$$

$$L = L_0 \log \frac{P}{4\pi r^2 I_0}$$

$$\boxed{L = 10 \text{ dB} \log \frac{P}{4\pi r^2 I_0}}$$

b) $L' = L_0 \log \frac{P}{4\pi (2r)^2 I_0}$ where $r' = 2r$

$$L' = L_0 \log \frac{P}{4\pi (2r)^2 I_0}$$

$$L' = L_0 \log \left[\left(\frac{P}{4\pi r^2 I_0} \right) \left(\frac{1}{4} \right) \right]$$

$$L' = L_0 \left[\log \left(\frac{P}{4\pi r^2 I_0} \right) + \log \left(\frac{1}{4} \right) \right]$$

$$L' = L_0 \log \frac{P}{4\pi r^2 I_0} + L_0 \log \frac{1}{4}$$

$$L' = L + 10 \text{ dB} \log \frac{1}{4}$$

$$L' = L - 6.0206 \text{ dB}$$

When you double the distance from the center of the source, the sound intensity level decreases by 6.0206 dB