

6) $I_1 = 15.0 \text{ dB}$

$$I_2 = \frac{1}{2} I_1 \Rightarrow \left(\frac{I_2}{I_1} = \frac{1}{2} \right)$$

a) $L_1 = 10 \text{ dB} \log \frac{I_1}{I_0}$

$$L_2 = 10 \text{ dB} \log \frac{I_2}{I_0}$$

$$\Delta L = L_2 - L_1$$

$$\Delta L = 10 \text{ dB} \log \frac{I_2}{I_0} - 10 \text{ dB} \log \frac{I_1}{I_0}$$

$$\Delta L = 10 \text{ dB} \left(\log \frac{I_2}{I_0} - \log \frac{I_1}{I_0} \right) = 10 \text{ dB} \log \frac{I_2/I_0}{I_1/I_0}$$

$$\Delta L = 10 \text{ dB} \log \frac{I_2}{I_1} = 10 \text{ dB} \log \left(\frac{1}{2} \right)$$

$$\boxed{\Delta L = -3.0103 \text{ dB}}$$

b) No. We found $\Delta L = 10 \text{ dB} \log \frac{I_2}{I_1}$ meaning the change depends only on the ratio of I_2 to I_1 , not on the value of I_1 . So, for instance, in the case given, $I_1 = 15 \text{ dB}$ and $I_2 = 7.5 \text{ dB}$ yielding $\Delta L = -3.0103 \text{ dB}$. But we would get the same result if I_1 were 40 dB and I_2 were 20 dB . Any pair of values such that $\frac{I_2}{I_1} = \frac{1}{2}$ works. It doesn't matter what I_1 is as long as $I_2 = \frac{1}{2} I_1$.